

Permittivity measurements at millimeter wave frequencies using dielectric rod resonator excited by NRD-guide

A. Nakayama*, H. Yoshikawa

R&D Center Kagoshima, Kyocera Corporation 1-4 Yamashita-cyo Kokubu, Kagoshima 899-4312, Japan

Available online 21 November 2005

Abstract

A method of measuring the relative complex permittivity ($\epsilon_r = \epsilon' - j\epsilon''$, $\tan \delta = \epsilon''/\epsilon'$) for low-loss dielectric materials at millimeter wave frequencies has been developed, using a dielectric rod resonator excited by the nonradiative dielectric waveguide (NRD-guide). Relative permittivity (ϵ') and loss factor ($\tan \delta$) of the rod specimen are determined by the resonant frequency (f_0) and unloaded Q-factor (Q_u) of a TE_{0m1} mode resonator. The effective conductivity (σ) of conducting plates for short-circuiting the rod resonator is determined using TE_{021} and TE_{028} mode sapphire resonators. Temperature dependence of ϵ' and $\tan \delta$ of sapphire and cordierite ceramics were evaluated at 60 GHz. This method has been adopted as the Japanese Industrial Standard (JIS R 1660-3) and is being prepared for the IEC international standard. Several standardized specifications are presented.

© 2005 Elsevier Ltd. All rights reserved.

Keywords: Dielectric properties; Electrical conductivity; Al_2O_3 ; Substrates; Millimeter wave measurements

1. Introduction

We need a reliable method for measuring ϵ_r of the dielectric materials for designing devices used in millimeter wave communication or sensing systems. Several methods^{1–4} have been developed for measuring ϵ_r of the low-loss dielectric materials at the millimeter wave frequencies. Among these methods, a dielectric rod resonator method excited by the NRD-guide⁵ has an advantage in that excitation of resonance is very easy. The reason is that a dominant LSM mode of the NRD-guide can be easily coupled to the TE mode of the dielectric resonator.

We have developed a simple and accurate method for measuring ϵ_r at millimeter wave frequencies based on the dielectric rod resonator excited by NRD-guide.⁶ The values of ϵ' and $\tan \delta$ are determined using the TE_{0m1} ($m = 1, 2, 3$) mode resonator. The TE_{0m1} mode resonator allows us to achieve stable measurements, and accurate and simple calculations for ϵ' and $\tan \delta$ by analytic expression. The effective conductivity σ of the conducting plates is determined using TE_{021} and TE_{028} mode sapphire resonators.

2. Theory and measurement formulas

2.1. Relative permittivity ϵ' and loss factor $\tan \delta$

The values of ϵ' and $\tan \delta$ of the rod specimen are determined using the TE_{0m1} mode resonator, as shown in Fig. 1a for $m = 2$. A dielectric rod with diameter (d) and height (h) is short-circuited at both ends by two parallel conducting plates.

The values of ϵ' is calculated from the measured f_0 , d and the space (h_c) between the upper and lower conducting plates:

$$\epsilon' = \left(\frac{\lambda_0}{\pi d} \right)^2 (u^2 + v^2) + 1 \quad (1)$$

where

$$v^2 = \left(\frac{\pi d}{\lambda_0} \right)^2 \left[\left(\frac{\lambda_0}{2h_c} \right)^2 - 1 \right] \quad (2)$$

Here, $\lambda_0 = c/f_0$ is the free space resonance wavelength and c is the velocity of light. A formula for u is given elsewhere.^{6,7}

Next, $\tan \delta$ is calculated from the measured Q_u :

$$\tan \delta = \frac{A}{Q_u} - BR_s = \frac{A}{Q_u} - \frac{B'}{\sqrt{\sigma_r}} \quad (3)$$

* Corresponding author.

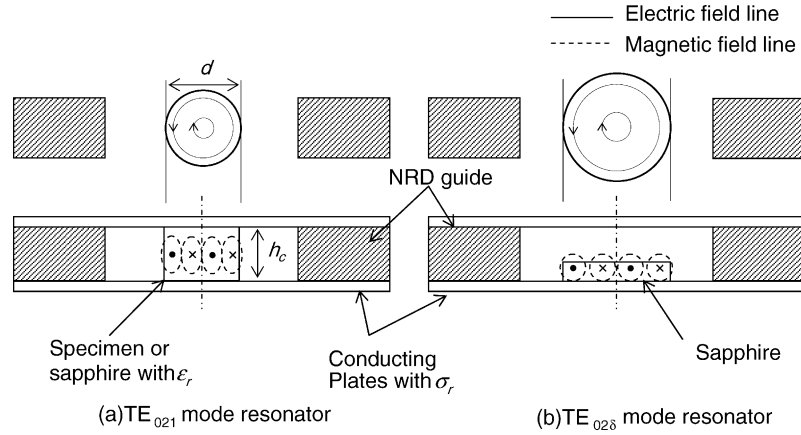


Fig. 1. Configuration of dielectric resonator for measuring ϵ_r and σ_r . Value of ϵ_r is measured using (a) and σ_r is measured using (a) and (b).

where

$$R_s(\Omega) = \sqrt{\frac{\pi f_0 \mu}{\sigma}} = \sqrt{\frac{\pi f_0 \mu}{\sigma_0 \sigma_r}} \quad (4)$$

Here, R_s and σ are the surface resistance and the effective conductivity of conducting plates, respectively. The relative conductivity is defined as $\sigma_r = \sigma/\sigma_0$ ($\sigma_0 = 5.8 \times 10^7$ S/m). Furthermore, μ is the permeability and $\mu = \mu_0 = 4\pi \times 10^{-7}$ for non-magnetic conducting plates. Formulas for A and B are given elsewhere.^{6,7}

2.2. Determination of relative conductivity σ_r of conducting plates

The value of σ_r of the conducting plates must be accurately measured, to determine $\tan \delta$ of low-loss dielectric specimen by (3). The TE_{021} and TE_{028} mode dielectric rod resonators in Fig. 1, called “standard resonators”, are used for measuring σ_r . Each standard resonator is made of sapphire single crystals with the same ϵ_r . They are designed to have the same f_0 .

The standard TE_{028} resonator has a large dimension ratio (d/h). The conductor loss of the TE_{028} resonator is larger than that of the TE_{021} standard resonator, since the electromagnetic field in the TE_{028} resonator is concentrated near the surface of the lower conductor. High accuracy measurement of σ_r is achieved by enlarging the difference in the conductor loss of the two resonators. While $f_{01} = f_{0\delta}$, Q_{u1} is higher than $Q_{u\delta}$, where subscripts 1 and δ denote each standard resonator.

The value of σ_r can be calculated from the measured f_0 ($=f_{01} = f_{0\delta}$), Q_{u1} and $Q_{u\delta}$:

$$\sigma_r = \frac{\sigma}{\sigma_0} = \pi \mu f_0 \left[\frac{Q_{u1} Q_{u\delta}}{G_1 G_\delta} \frac{G_1 P_{e1} - G_\delta P_{e\delta}}{Q_{u1} P_{e1} - Q_{u\delta} P_{e\delta}} \right]^2 / \sigma_0 \quad (5)$$

where partial electric energy filling factors (P_{e1}) and ($P_{e\delta}$), and geometric factor (G_1) and (G_δ) of the resonators are defined elsewhere.⁶ An example of their values is shown in Table 1.

Furthermore, $\tan \delta$ of the standard resonators can be calculated:

$$\tan \delta_1 = \tan \delta_\delta = \frac{1}{Q_{u1} Q_{u\delta}} \times \frac{G_1 Q_{u\delta} - G_\delta Q_{u1}}{G_1 P_{e1} - G_\delta P_{e\delta}} \quad (6)$$

3. Preparation of dielectric specimen

Typical specifications of the standard rod resonators are described. Each rod consists of the sapphire with low $\tan \delta$. The axis of the each rod is parallel to the C -axis of sapphire. Table 1 shows d , h , h_c , P_e and G of the standard sapphire rods with $\epsilon' = 9.40$ perpendicular to the C -axis, for measuring σ_r at 60 GHz. The factors P_{e1} and G_1 are related with A and B in (3) by $P_{e1} = 1/A$ and $G_1 = A/B$. In contrast, calculations for factors $P_{e\delta}$ and G_δ require numerical analyses. Table 1 shows values of $P_{e\delta}$ and G_δ obtained by axis symmetric FEM calculations.

The TE_{011} , TE_{021} and TE_{031} mode rod resonators are used to measure ϵ' and $\tan \delta$, for materials with $\epsilon' = 2-4$, $\epsilon' = 4-20$ and $\epsilon' = 20-30$. Fig. 2 shows desirable values of diameter (d) of the rod specimen for 60 GHz measurement as a function of ϵ' .

4. Measurement apparatus

Two types of apparatus were used, as shown in Fig. 3. The dielectric rod resonator was coupled equally to the input and output NRD-guide. Space between the rod and the NRD-guide was adjusted so that insertion loss (IL_0) at f_0 was 20–25 dB. Dielectric strips of the NRD-guide with a width of 2.00 mm were made of Rexolite-1422 (cross-linked styrene copolymer) with $\epsilon' = 2.5$,

Table 1
Dimensions, partial electric energy filling factor P_e and geometric factor G for standard sapphire rods for measuring σ_r at 60 GHz.

| Space, h_c (mm) | TE ₀₂₁ | | | | TE ₀₂₈ | | | |
|-------------------|--------------------|------------------|----------|--------------------|-------------------|----------|---------------|-------------------------|
| | Diameter, d (mm) | Height, h (mm) | P_{e1} | G_1 (Ω) | d (mm) | h (mm) | $P_{e\delta}$ | G_δ (Ω) |
| 2.25 | 3.14 | 2.20–2.25 | 0.915 | 1182 | 4.49 | 0.80 | 0.906 | 409 |

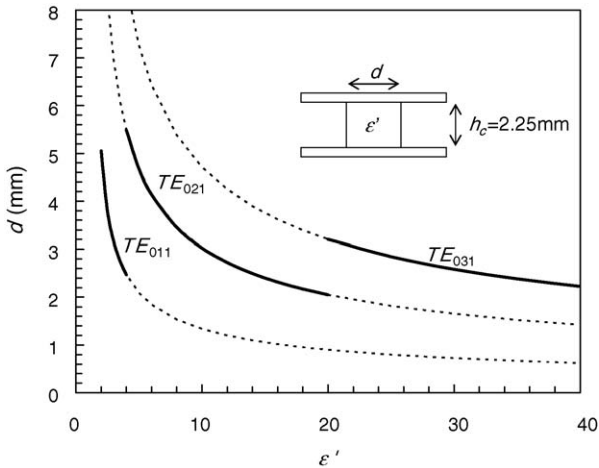


Fig. 2. Diameter d of dielectric specimen for measuring ϵ_r at 60 GHz, for height $h = 2.20\text{--}2.25$ mm and space $h_c = 2.25$ mm.

for 60 GHz measurements. The apparatus had transducers from the NRD-guide to the waveguide. The end of the dielectric strip was sharpened in the transducer.

A-type apparatus was used for measuring the temperature dependence of $\tan \delta$, since the $TE_{02\delta}$ standard resonator is easily constituted. The upper conducting plate was inset in the con-

ductors of NRD-guide in the A-type apparatus. The apparatus had a small air gap (g) between the upper conducting plate and the dielectric specimen. The calculations of ϵ' by (1) and of $\tan \delta$ by (3) are accurate for $g < 50 \mu\text{m}$. The error of $\Delta\epsilon'/\epsilon'$ for $g = 50 \mu\text{m}$ is about 0.01% and is negligible.⁶ In contrast, B-type apparatus was used for measuring the temperature dependence of ϵ' . The upper conducting plate was put on the specimen in this apparatus.

The apparatus was connected to a scalar network analyzer HP-8757 system. The Q_u was calculated from f_0 , the half-power band width $f_H - f_L$ and IL_0 :

$$Q_u = \frac{f_0 / (f_H - f_L)}{(1 - 10^{-IL_0/20})} \quad (7)$$

5. Results

The temperature (T) dependence of ϵ_r of sapphire and cordierite ceramics⁸ was evaluated at 60 GHz by this method. First, f_0 was measured as a function of T using the B-type apparatus. Then ϵ' was calculated from the f_0 . Fig. 4a shows ϵ' and f_0 of the TE_{021} standard sapphire rod ($d = 3.130 \pm 0.005$ mm, $h = 2.250 \pm 0.001$, $\alpha = 5.8$ ppm/ $^\circ\text{C}$). Here, α is the coefficient of thermal expansion. The values ϵ' of the sapphire increased linearly with increasing T . The first and second

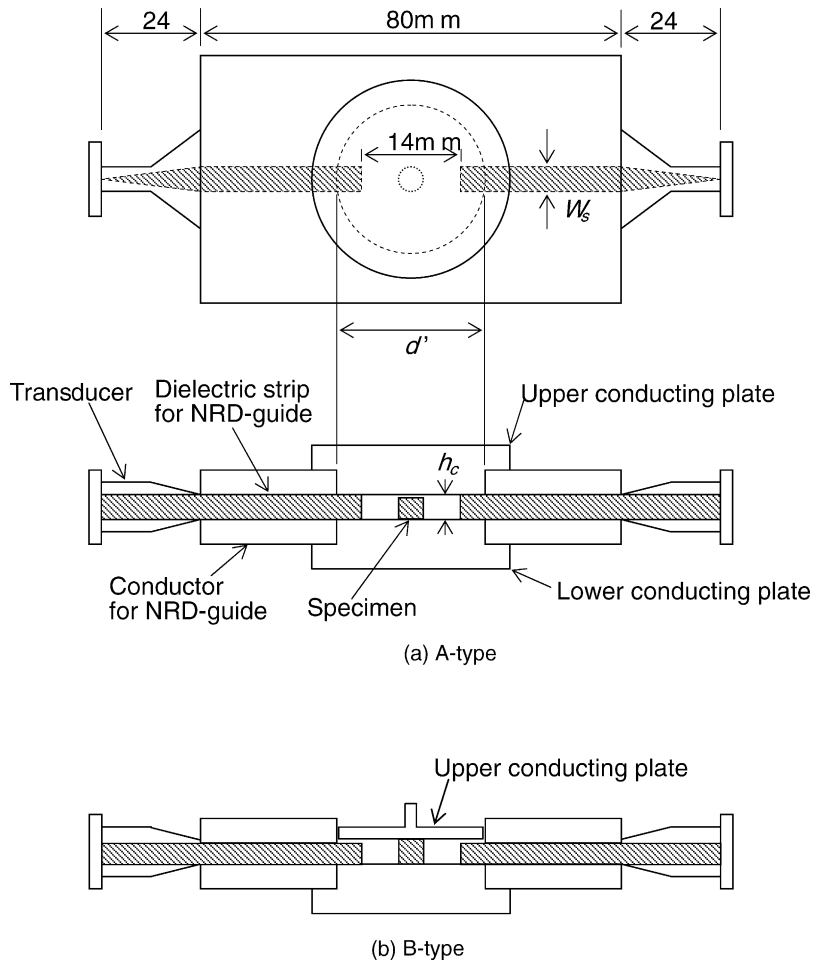


Fig. 3. Measurement apparatus.

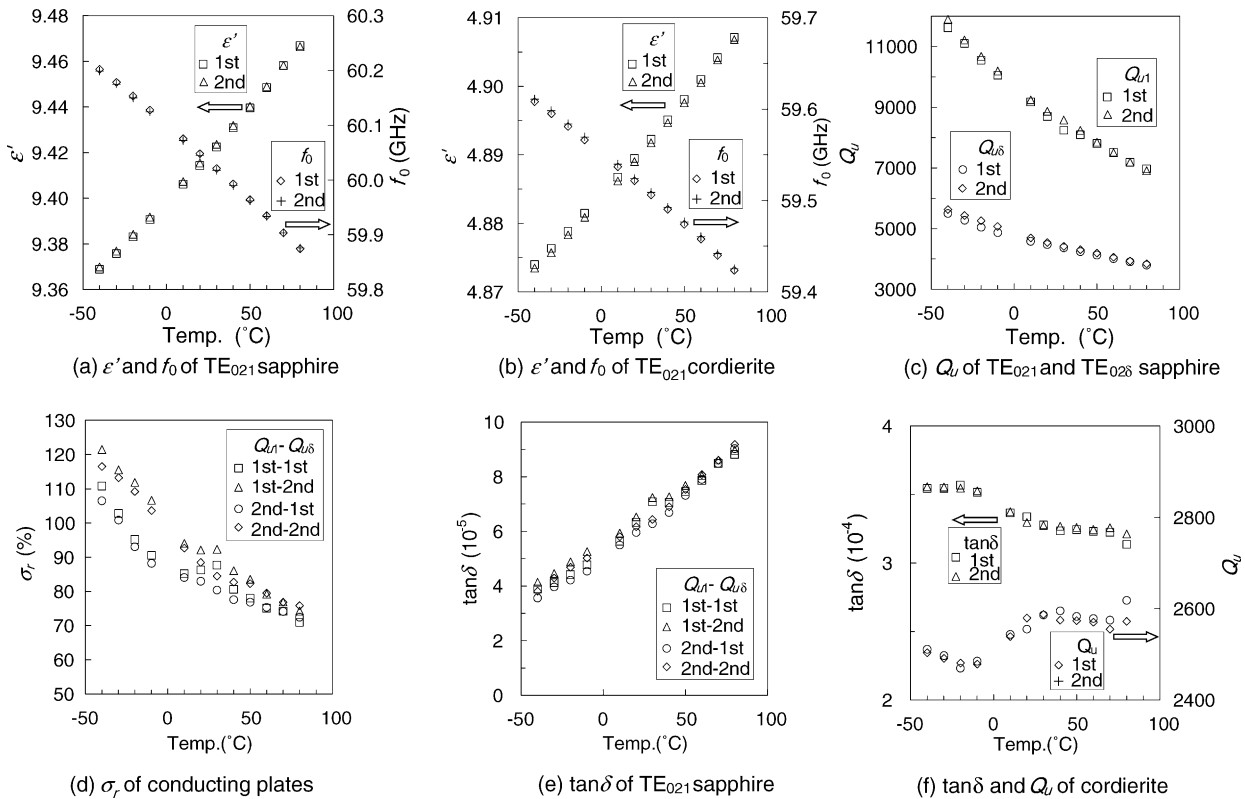


Fig. 4. Temperature dependence measurements of ϵ_r of sapphire crystals and cordierite ceramics, and of σ_r of conducting plates.

measurements were in agreement. The temperature coefficient of permittivity ($TC\epsilon$) of the sapphire was calculated to be 86.4 ± 0.8 ppm/°C, which was in good agreement with a result reported elsewhere.⁹ Fig. 4b shows measurements of cordierite ceramics rod ($d=4.803$, $h=2.253$, $\alpha=0.5$). The values ϵ' of the cordierite rod also increased linearly with increasing T . The value $TC\epsilon$ was calculated to be 56.9 ± 0.3 ppm/°C.

Next, to determine σ_r of the conducting plates of Cu and $\tan\delta$ of the standard sapphire, Q_{u1} and $Q_{u\delta}$ of standard sapphire resonators was measured twice against T as shown in Fig. 4c, using the A-type apparatus with $H_c=2.279$ mm. Fig. 4d and 4e show σ_r of the conducting plates and $\tan\delta$ of the standard sapphire calculated by Q_{u1} and $Q_{u\delta}$. The value of σ_r decreased with increasing T . The value σ_r was 87.4% at 20 °C. The value $\tan\delta$ of the standard sapphire increased with increasing T . The value $f_0/\tan\delta=1.04 \times 10^6$ GHz at 20 °C was in agreement with a result reported elsewhere.⁶ Furthermore, Fig. 4f shows Q_u and $\tan\delta$ of cordierite ceramics. This variation of $\tan\delta$ with T was relatively small.

6. Conclusion

A method of measuring ϵ_r at millimeter wave frequencies has been developed, using a dielectric resonator excited by the NRD-guide. Typical specifications of the rod specimen for ϵ_r measurements and of the standard sapphire rods for measuring σ_r at 60 GHz were presented. The temperature dependence of ϵ_r of sapphire and cordierite ceramics was accurately evaluated

at 60 GHz by this method. The repeated measurements showed the error of $TC\epsilon$ was less than 1 ppm/°C.

References

- Cullen, A. L. and Yu, P. K., The accurate measurement of permittivity by means of an open resonator. *Proc. Roy. Soc. A*, 1971, **325**, 493–509.
- Kobayashi, Y. and Shimizu, T., Millimeter wave measurement of temperature dependence of complex permittivity of dielectric plates by a cavity resonance method. *IEEE MTT-S Int. Microwave Symp. Digest*, 1999, 1885–1888.
- Y. Ishikawa, T. Tanizaki, A. Saitoh, and T. Yoneyama, Complex permittivity measurement of dielectric materials using NRD guide at millimeter wave length. *IEICE Trans. C-I Vol. J78-C-I*, 9, 1995, pp. 418–429 (in Japanese).
- Krupka, J., Derzakowski, K., Abramowicz, A., Tobar, M. E. and Geyer, R. G., Use of whispering-gallery modes for complex permittivity determinations of ultra-low-loss dielectric materials. *IEEE Trans. Microwave Theory Tech.*, 1999, **47**, 752–759.
- Yoneyama, T. and Nishida, S., Nonradiative dielectric waveguide for millimeterwave integrated circuit. *IEEE Trans. Microwave Theory Tech.*, 1981, **29**, 1188–1192.
- Nakayama, A., Fukuura, A. and Nishimura, M., Millimeter-wave measurement of complex permittivity using dielectric rod resonator excited by NRD-guide. *IEEE Trans. Microwave Theory Tech.*, 2003, **51**, 170–177.
- Kobayashi, Y. and Katoh, M., Microwave measurement of dielectric properties of low-loss materials by the dielectric rod resonator method. *IEEE Trans. Microwave Theory Tec.*, 1985, **33**, 586–592.
- Hiramatsu, N., Kishino, T., Okamura, T., Kii, H. and Sagala, D. A., Non-radiative dielectric waveguide using cordierite ceramics. *IEEE MTT-S Int. Microwave Symp. Digest*, 1999, 1785–1788.
- Kobayashi, Y. and Tamura, H., Round robin test on a dielectric resonator method for measuring complex permittivity at microwave frequency. *IEICE Trans. ELECTRON. E77-C*, 1994, **6**, 882–887.